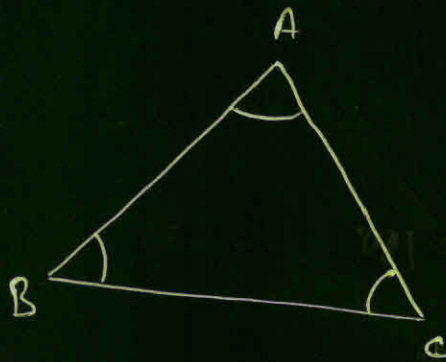


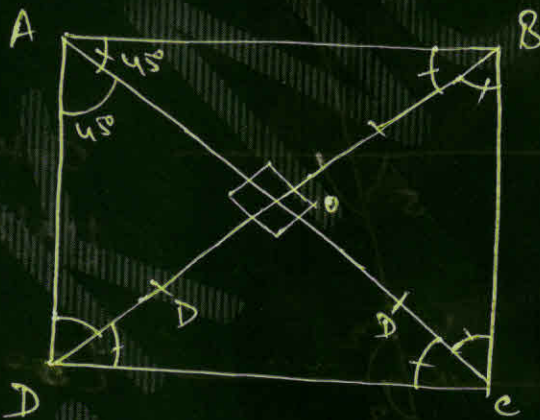
* — Geometry — *

⇒ Triangle :-



$$\angle A + \angle B + \angle C = 180^\circ$$

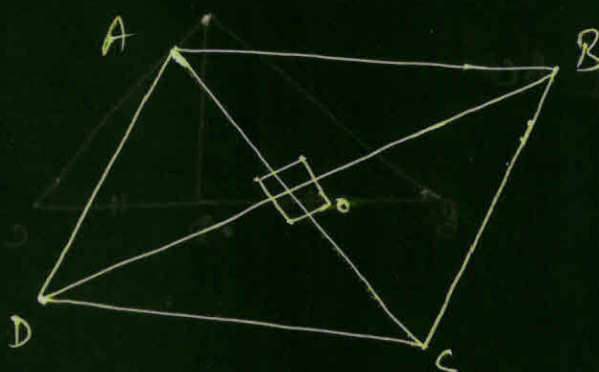
⇒ Square :-



Diagonal :- $AC = BD = \sqrt{2}a$

Area = $a \times a$.

⇒ Rhombus :-



$$AB = BC = CD = DA$$

$$AC \neq BD$$

$$\text{Area} = \frac{1}{2} \times D_1 \times D_2$$

$$\angle A = \angle C$$

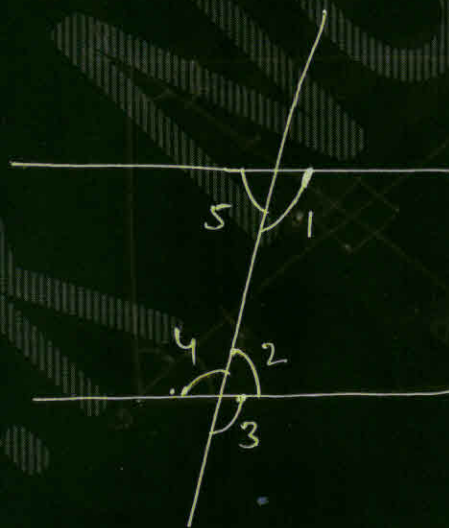
$$\angle B = \angle D$$

$$\angle A + \angle B = 180^\circ$$

$$\angle B + \angle C = 180^\circ$$

$$\angle C + \angle D = 180^\circ$$

$$\angle D + \angle A = 180^\circ$$



Interior angle =

$$\angle 1 + \angle 2 = 180^\circ$$

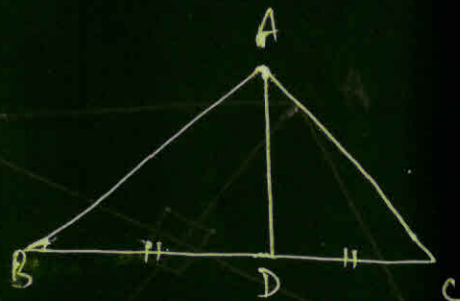
$\angle 3 = \angle 4 =$ Corresponding Angle.

$\angle 2 = \angle 5$ Alternate Interior Angle.

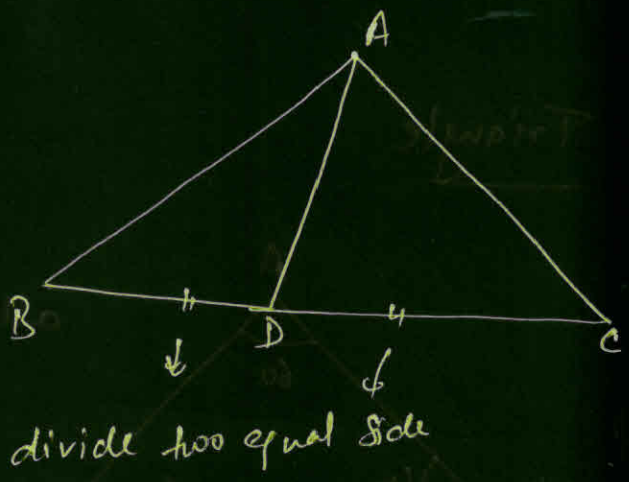
$\angle 1 = \angle 7$ Alternate Exterior Angle.

① Perpendicular i-

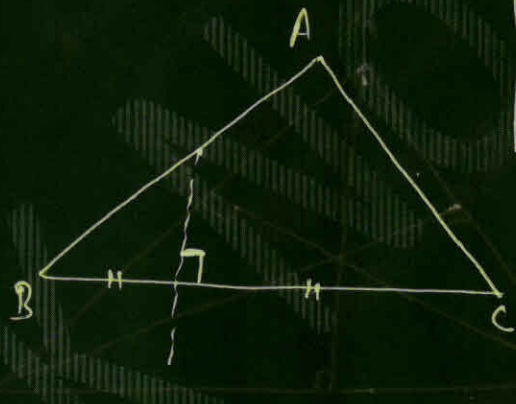
$$AD \perp BC$$



② Median :-

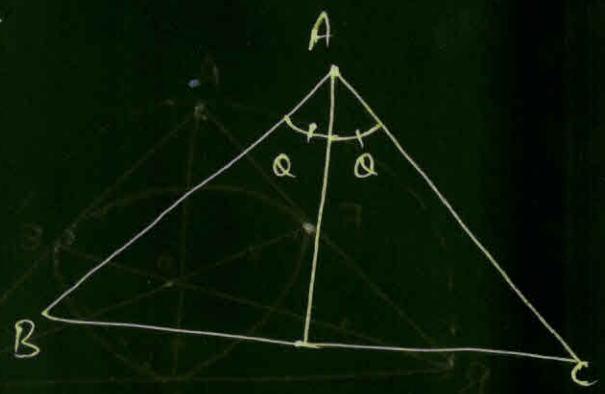


③ Perpendicular Bisector :-



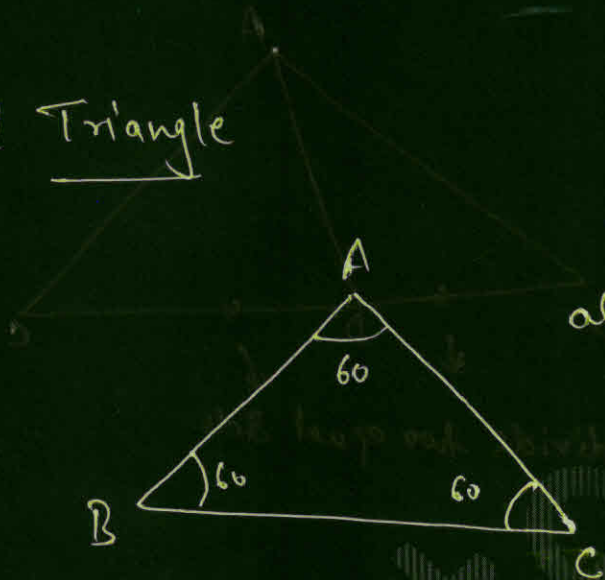
Equilateral Δ
 isosceles Δ

④ Angle Bisector :-



Triangles:

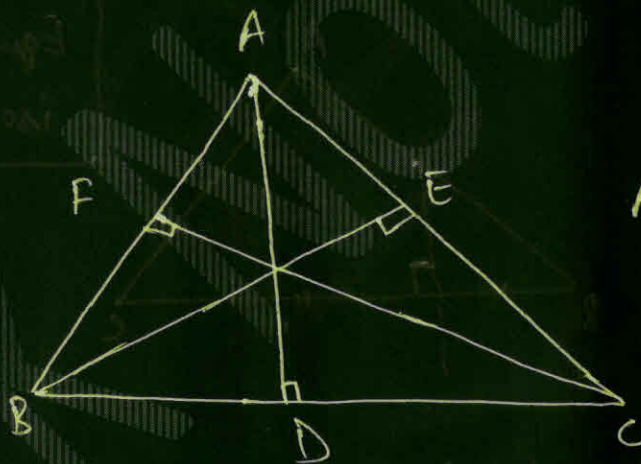
① Equilateral Triangle



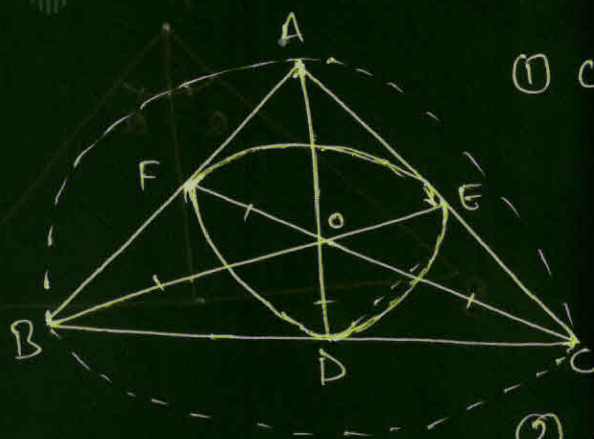
all Angle & all side will be equal.

$$\text{Area} = \frac{\sqrt{3}}{4} a^2$$

$$\text{Height} = \frac{\sqrt{3} a}{2}$$



$$AD = BE = CF$$



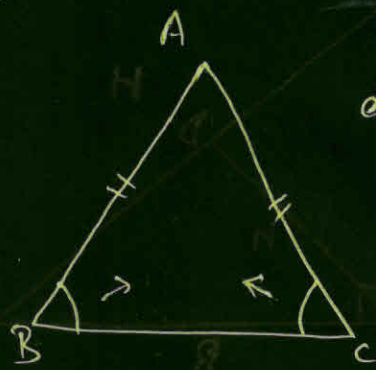
$$\textcircled{1} \text{ Circum Radius } (R) = \frac{a}{\sqrt{3}}$$

$$OA = OB = OC$$

$$\textcircled{2} \text{ In-Radius } (r) = \frac{a}{2\sqrt{3}}$$

$$OD = OE = OF$$

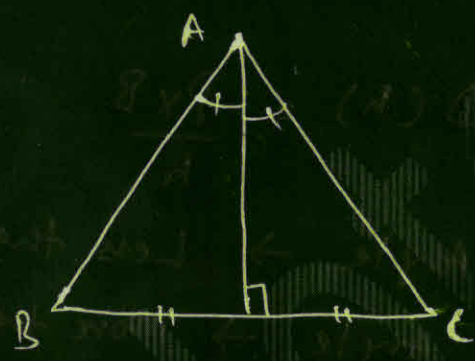
② Isosceles triangle:-



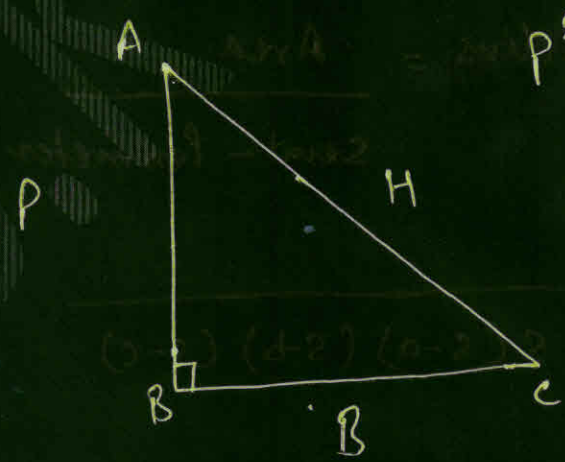
$$\text{area} = \frac{1}{2} \times AB \times AC \times \sin A$$

$$AB = AC$$

$$\angle B = \angle C$$



③ Right Angle triangle:-



$$P^2 + B^2 = H^2$$

⇒ Right Angle Δ is one angle equal to 90°

⇒ Some Trigonometry Triplet No.

3, 4, 5

9, 12, 15

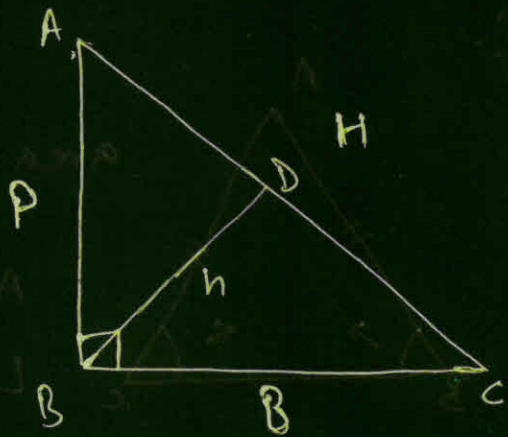
6, 8, 10

7, 24, 25

60, 80, 100

5, 12, 13





$$(AB)^2 = AD \times AC$$

$$(BC)^2 = CD \times AC$$

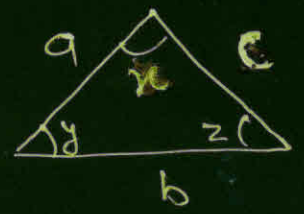
$$(BD)^2 = AD \times CD$$

$$BD(h) = \frac{p \times q}{h}$$

- Acute Angle → Less than 90°
- obtuse Angle → More than 90°
- Circum - Radius = $\frac{a \times b \times c}{4 \times \text{Area}}$

$$\rightarrow \text{In - Radius} = \frac{\text{Area}}{\text{Semi - Perimeter}}$$

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$$



$$s = \frac{a + b + c}{2}$$

Q: Triangle A, B, C is an isosceles Triangle with Angle $C = 90^\circ$. $AC = 5 \text{ cm}$. find AB .

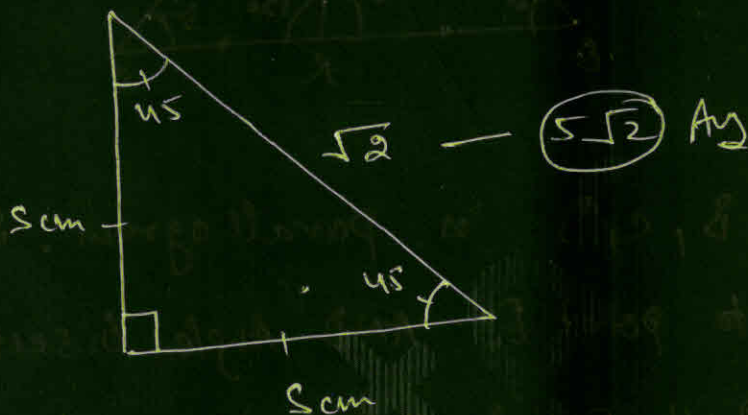
Solⁿ:

$$H^2 = P^2 + B^2$$

$$H^2 = 25 + 25$$

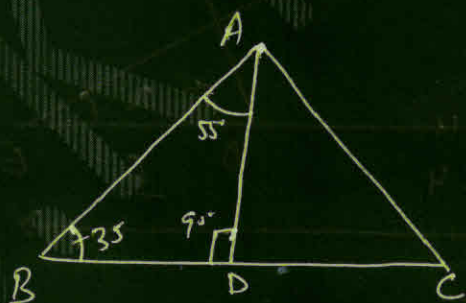
$$H^2 = 50$$

$$H = 5\sqrt{2} \text{ cm}$$



Q: A, B, C is isosceles angle such that $AB = AC$ and $\angle B$ is 35° . AD is median on side BC find $\angle BAD$.

Solⁿ:



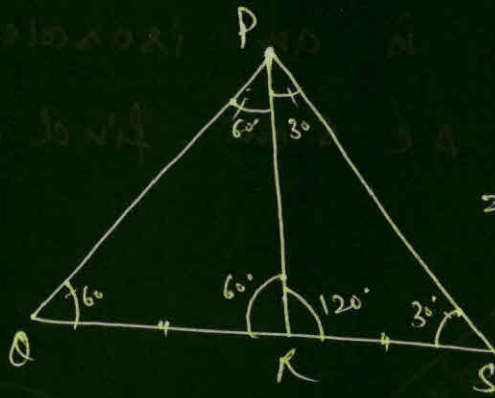
$$\triangle \Rightarrow 180^\circ$$

$$35 + 90 + A = 180$$

$$A = 180 - 125 = 55^\circ \text{ Ans}$$

Q: P, Q, R is equilateral Δ in which side QR is produced upto point S in such a way that $QR = RS$. find the Angle $\angle PSR$.

Ans:

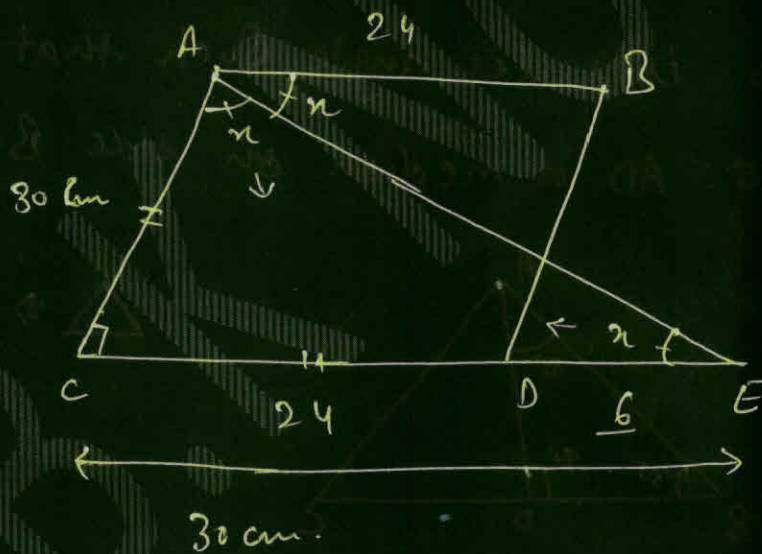


$$\begin{aligned}
 60 + 60 &= 120^\circ \\
 30 + 30 &= 60^\circ \quad \rightarrow 180^\circ \\
 &= \textcircled{30} \text{ Ans}
 \end{aligned}$$



Q1:- A, B, C, D is parallelogram. Side CD is extended upto point E. AND Angle bisector of Angle B meets Point E. find DE if AB 24 cm and BC 30 cm.

Solⁿ:-



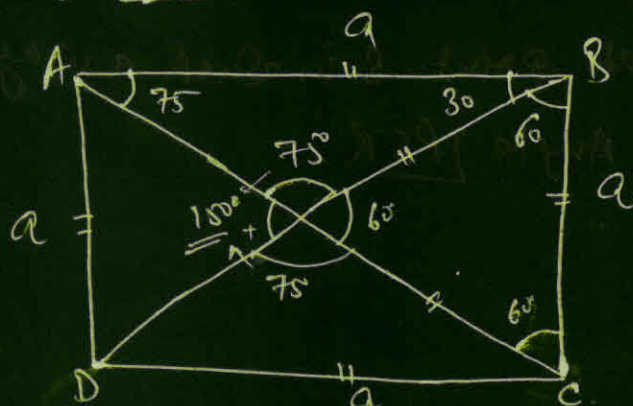
= 6 Ans

Q2:- A, B, C, D is a Square on side BC and equilateral Δ . ΔBEC is drawn inside a Square find Ang \underline{AED} .

Solⁿ:-



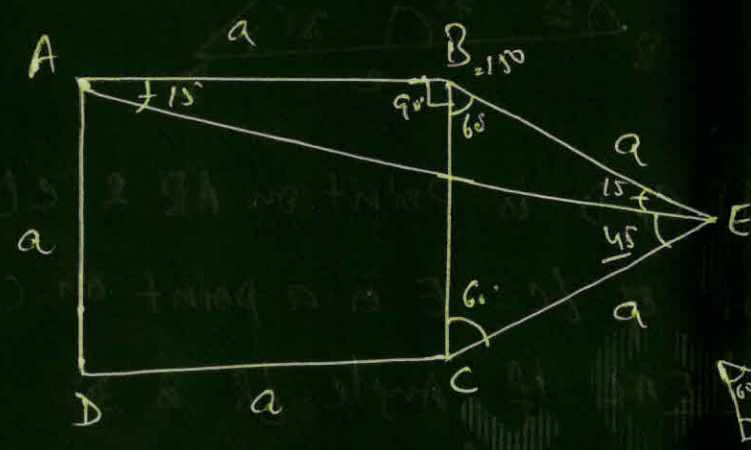
$$\begin{aligned}
 360 - 210 \\
 = 150
 \end{aligned}$$



150 Ans

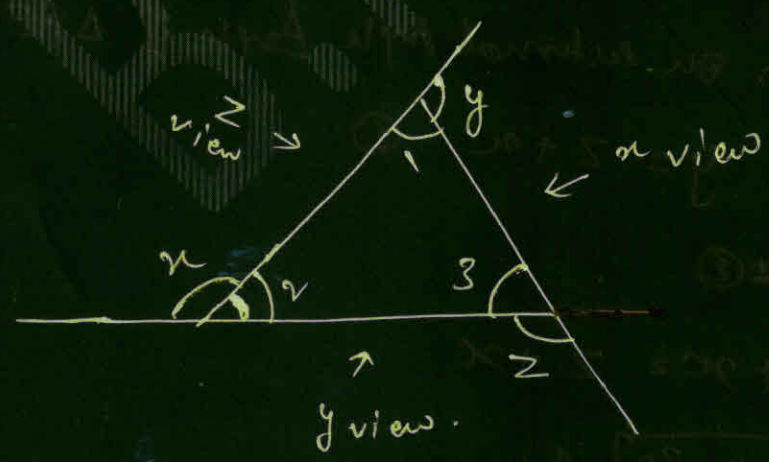
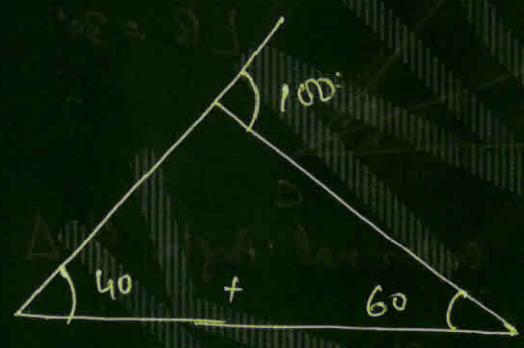
Q: ABCD is square on side BC Equilateral Δ . ΔBEC is drawn outside of square find the $\angle AEC$.

Soln:



45° Ans

Q:



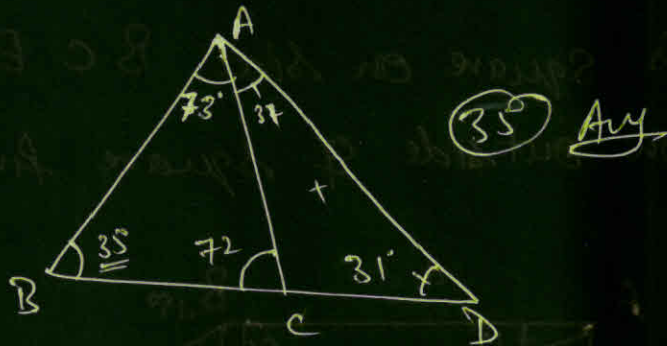
$$x = 1 + 3$$

$$y = 2 + 3$$

$$z = 1 + 2$$

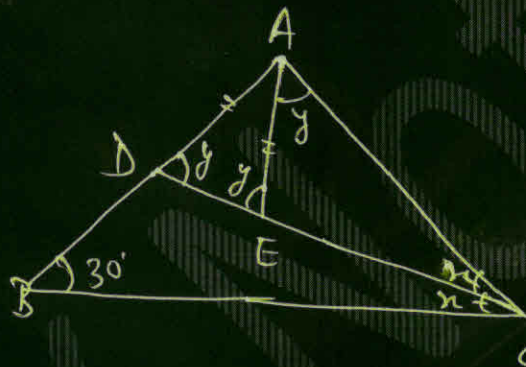
Q: In a ΔABC side BC is extended upto point D. Such that $CD = AC$ if $\angle BAD$ is 109° . $\angle ACB$ is 72° then find $\angle ABC = ?$

Soln:



Q: In $\triangle ABC$, D is point on AB & CD is an Angle Bisector of $\angle C$. E is a point on CD & $AD = AE$. Find $\angle EAC$ if Angle $\angle B$ is 30° .

Soln:



$\angle EAC = ?$

$\angle B = 30^\circ$

$\angle ADE$ is an external angle of $\triangle DBC$

$$y = 30 + x \quad \text{--- (1)}$$

$\angle AED$ is an external angle of $\triangle AEC$.

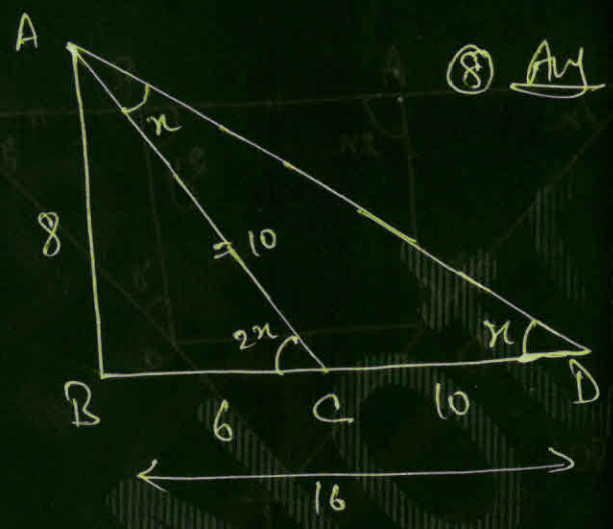
$$y = z + x \quad \text{--- (2)}$$

$$\text{(1) } \pm \text{(2)}$$

$$30 + x = z + x$$

$$\boxed{z = 30} \text{ Ans}$$

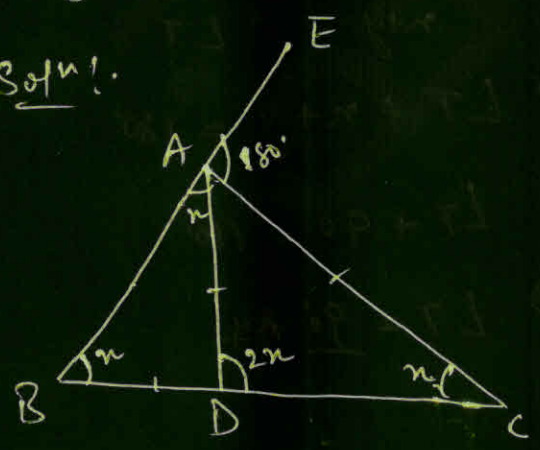
Q1. ABC is right angle triangle in which B is Right Angle. Side BC is extended upto point D. Such that $\angle ADB$ is half of $\angle ACB$. if $BD = 16\text{ cm}$ & $CD = 10\text{ cm}$ then find AB.



Q2. In a $\triangle ABC$, D is point BC such that $AD = BD = AC$ side BA is extended upto point E. If Angle $\angle CAE = 80^\circ$. find Angle C.

$\angle CAE = 80^\circ$
 $AD = BD = AC$
 $\angle C = ?$

Solⁿ!



$\angle CAE = \angle B + \angle C$

$80 = x + 2x$

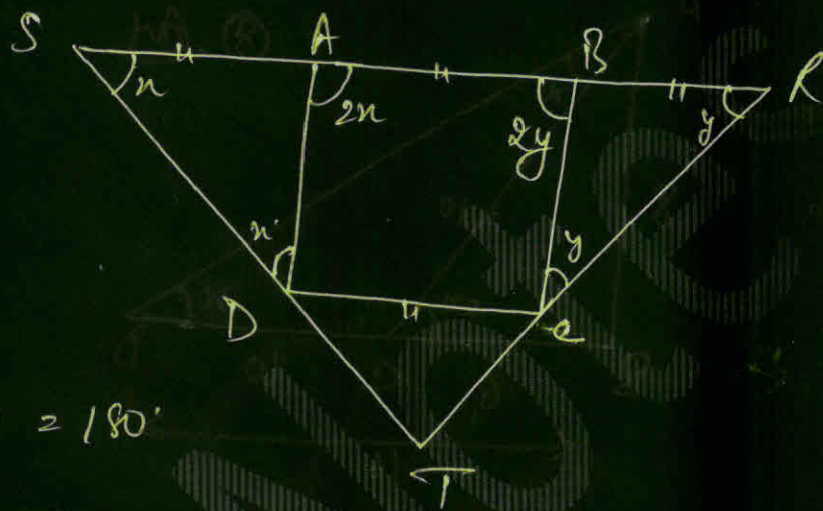
$x = \frac{80}{3}$

$\angle C = 2x \Rightarrow 2 \times \frac{80}{3}$

$x = \left(\frac{160}{3}\right)$ Ans

Q:- A, B, C, D is Rhombus side AB and BA are extended upto point R & the extended parts of side RC & SD meets at points T . if $SA = AB = BR$ then find $\angle T = ?$

Soln:-



$$2x + 2y = 180^\circ$$

$$x + y = 90^\circ$$

In ΔSTR

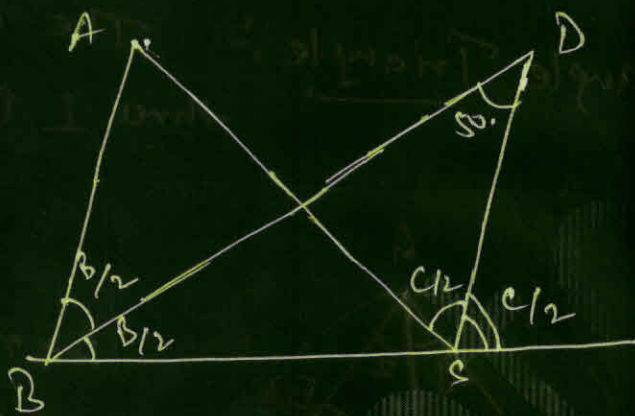
$$\Rightarrow \frac{\angle S + \angle R}{x + y} + \angle T$$

$$\Rightarrow \angle T + x + y = 180^\circ$$

$$\Rightarrow \angle T + 90^\circ = 180^\circ$$

$$\Rightarrow \angle T = \underline{90^\circ} \text{ Ans}$$

Q1:- The Angle bisector of Internal $\angle B$ & external $\angle C$ of ΔABC meets each other at point D . $\angle D$ is 50° then find the $\angle A = ?$



$$\angle C = \angle A + \angle B$$

$$\frac{\angle C}{2} = \frac{\angle B}{2} + 50$$

$$\angle C = \angle B + 100$$

$$\cancel{A} + \angle B = \cancel{B} + 100$$

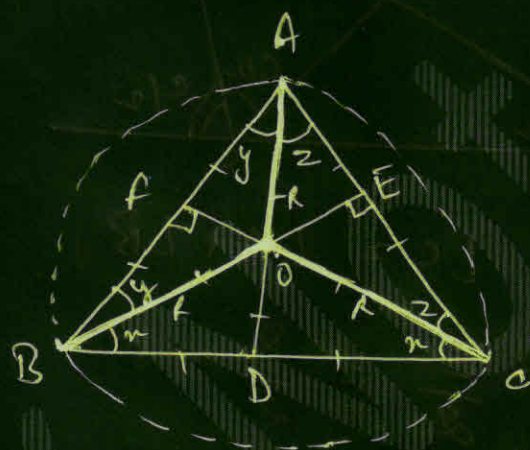
$$\boxed{\angle A = 100} \quad \underline{A_1}$$



* Centres of Triangle :-

① Circum Centre :- The common point of all three \perp Bisector of Triangle.

① Acute angle Triangle :- The common point of three \perp Bisector of a Δ .



$$A + x = 90^\circ$$

$$C + y = 90^\circ$$

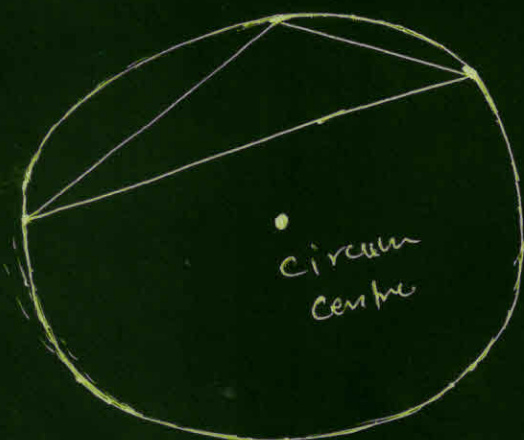
$$B + z = 90^\circ$$

$$AO = BO = CO =$$

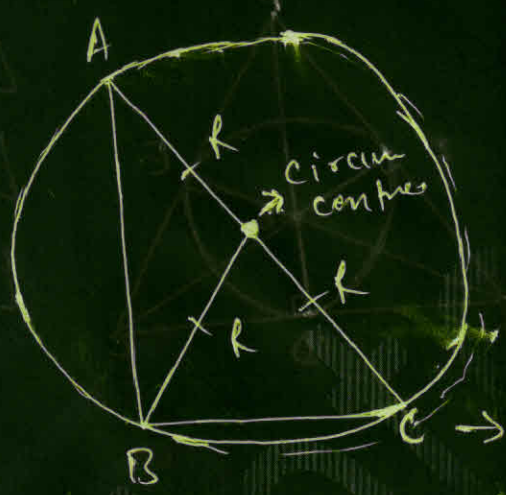
Circum Radius

② obtuse Angle Δ :-

In obtuse Angle Δ the Circum Centre will be outside the Δ .



③ Right Angle triangle: In a right angle Triangle Δ the circum centre will be at the mid of Hypotenuse.

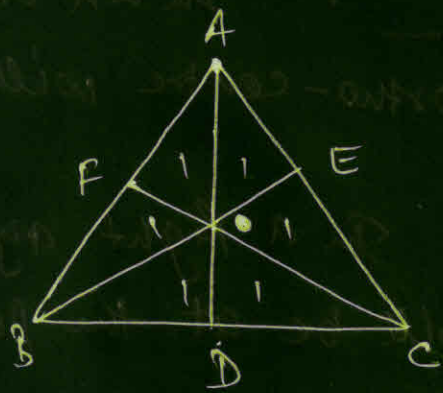


\rightarrow C always touch Circum centre.

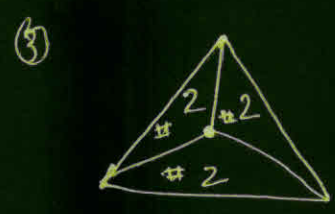
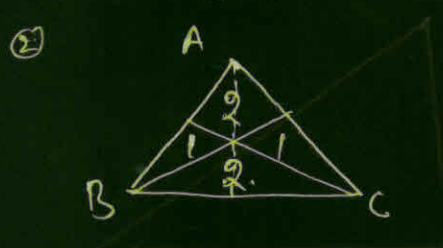
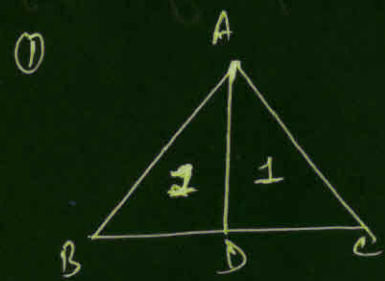
\rightarrow Each & every angle drawn by the diameter in the semicircle will always be 90°

④ Centroid

\rightarrow A common point drawn by all three medians of a Δ .

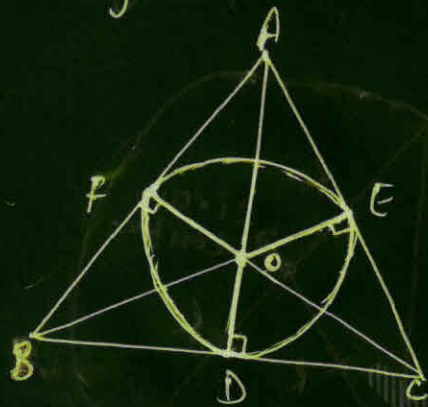


$AO : OD$
 $BO : OE$
 $CO : OF$
 $2 : 1$



③ In-Centre :-

→ A Common point of all three Angle Bisectors of Triangle Δ .



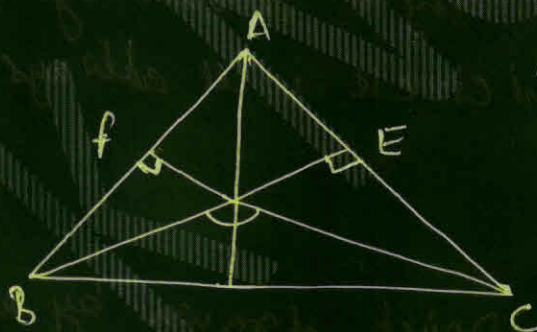
$$\angle BOC = 90^\circ + \frac{\angle A}{2}$$

$$\angle AOB = 90^\circ + \frac{\angle C}{2}$$

$$\angle AOC = 90^\circ + \frac{\angle B}{2}$$

④ Ortho Centre :-

① → A Common point of all three \perp of a Δ .



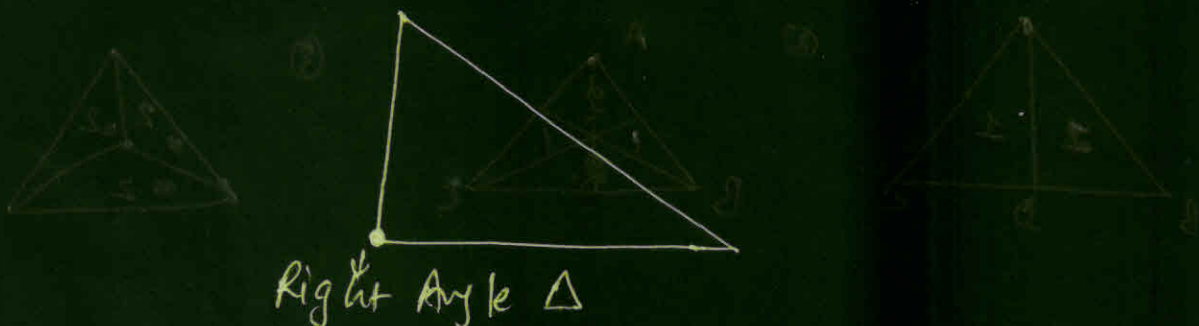
$$\angle A + \angle BOC = 180^\circ$$

$$\angle B + \angle AOC = 180^\circ$$

$$\angle C + \angle AOB = 180^\circ$$

② Obtuse Angle Δ :- In an obtuse Angle Δ the ortho-centre will be outside the Δ .

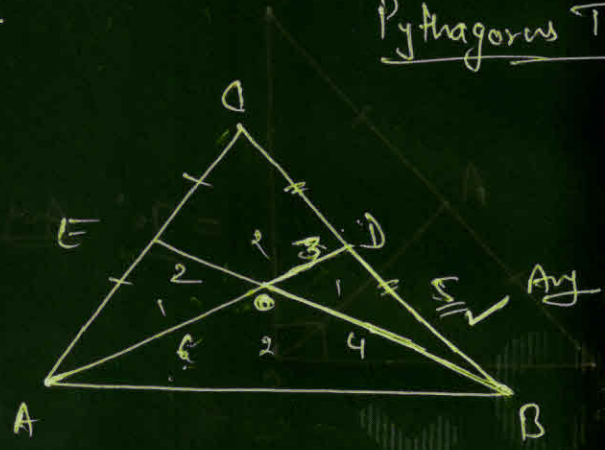
③ Right Angle Δ :- In a Right angle Δ the ortho centre will be at the point of right angle.



Right Angle Δ

Q: Two median AD & BE of ΔABC intersect each other at right angle. If AD = 4 cm & BE = 3 cm then find BD.

Solⁿ:



Pythagoras Triplet:

$$(OB)^2 + (OD)^2 = (BD)^2$$

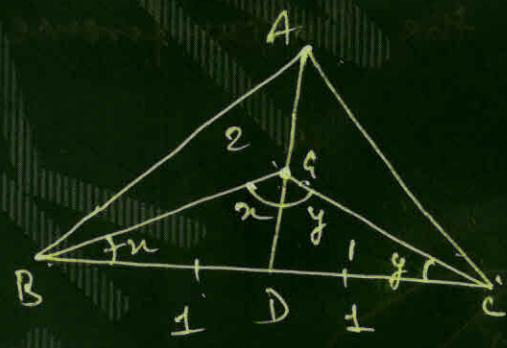
$$(1)^2 + (3)^2 = (BD)^2$$

$$1 + 9 = (BD)^2$$

$$10 = (BD)^2$$

$$BD = \sqrt{10} \text{ cm}$$

Q: In a triangle ABC and G is centroid such that $AG = BC$ find $\angle BGC$.



$AG = BC = 2$
 ΔBGC

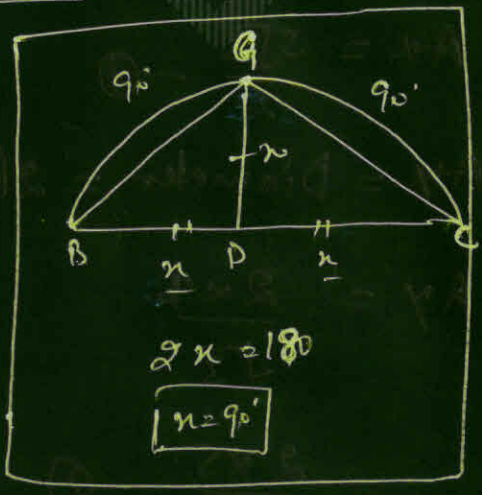
$$\angle B + \angle G + \angle C = 180^\circ$$

$$x + x + y + y = 180^\circ$$

$$2x + 2y = 180^\circ$$

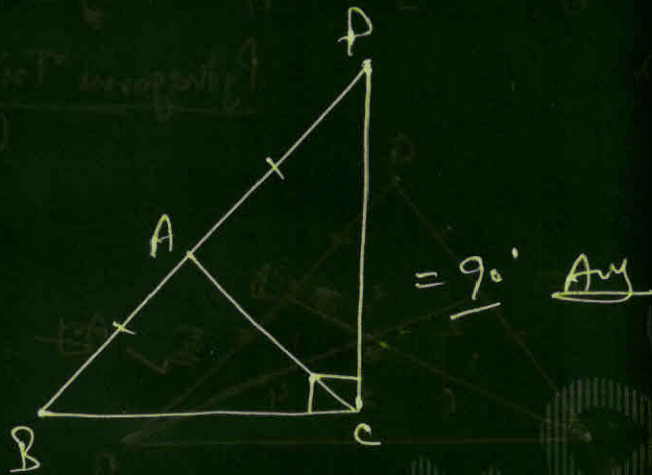
$$x + y = 90^\circ$$

Trick



Q1) In a $\triangle ABC$, $AB = AC$ the side BA is extended upto point P. Such that $AP = AC$. find $\angle PCB = ?$

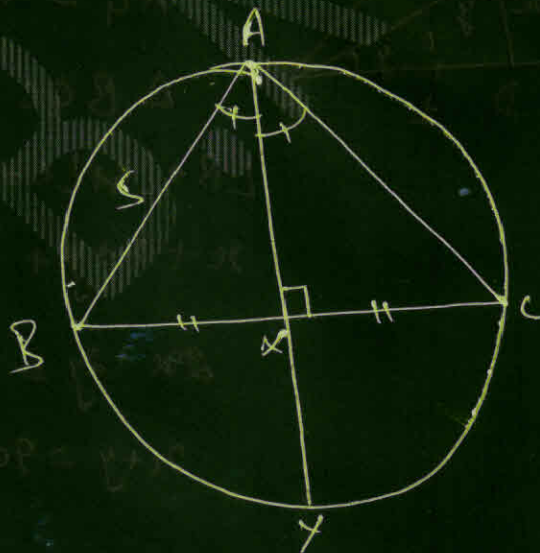
Solⁿ:-



$= 90^\circ$ Ans

Q2) ABC is an equilateral \triangle drawn inside a circle $AB = 5$ cm. the Bisector of Angle A, meets BC at point X & the Circumference at point Y. find AX into AY.

Solⁿ:-



$$AX = \frac{\sqrt{3}}{2} a$$

$$AX = \frac{5\sqrt{3}}{2} \quad \text{--- (1)}$$

$$AY = \text{Diameter} = 2R$$

$$AY = \frac{2 \times r}{\sqrt{3}}$$

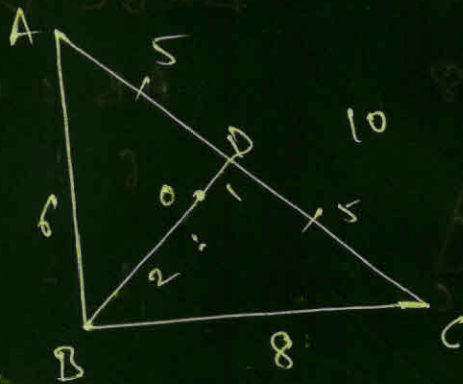
$$\frac{2 \times 5}{\sqrt{3}} \quad \text{--- (2)}$$

$$AX \cdot AY$$

$$\frac{5\sqrt{3}}{2} \times \frac{2 \times 5}{\sqrt{3}} = \underline{25} \text{ Ans}$$

Q1: In a ΔABC $AB = 6\text{ cm}$, $BC = 8\text{ cm}$ & $AC = 10\text{ cm}$
 O is the centroid. find $BO = ?$

Solⁿ



always use $2:1$ when
 Point nearest on Second
 Point.

$$BO : OD$$

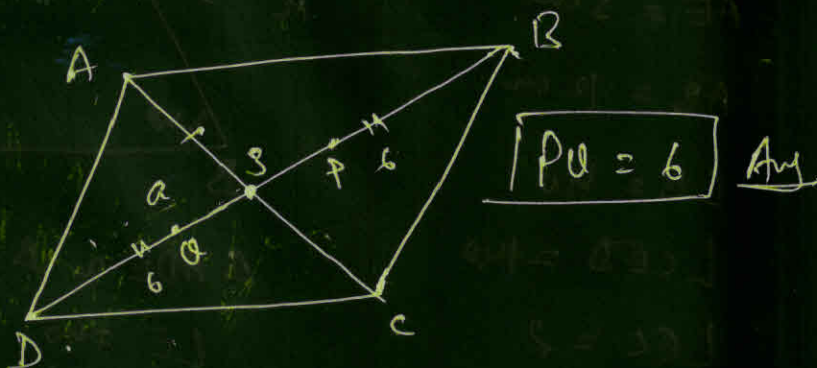
$$2 : 1 = 3 \times \frac{5}{3}$$

$$\frac{5}{3}$$

$$\left(\frac{10}{3}\right) \text{ Ans}$$

Q6: the length of diagonal BD of $\parallel\text{gm } ABCD$ is 18 cm
 P & Q are centroid of ΔABC & ADC .
 find the length $PQ = ?$

Solⁿ



$$\boxed{PQ = 6} \text{ Ans}$$

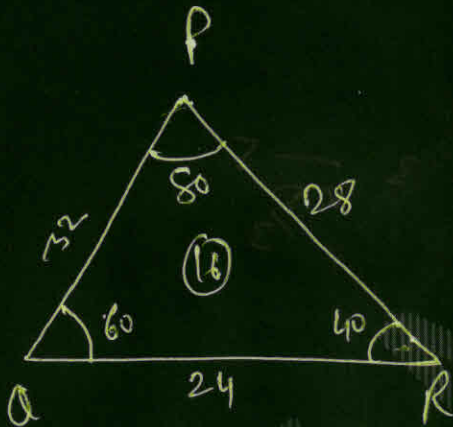


$$\triangle ABC \sim \triangle PQR$$

$$AB = QR$$

$$6 = 24$$

$$1 = 4$$



$$\frac{\text{Area of } \triangle ABC}{\text{Area of } \triangle PQR} = \left(\frac{AB}{QR}\right)^2 = \left(\frac{BC}{PR}\right)^2 = \left(\frac{AC}{PQ}\right)^2$$

Q1- In a $\triangle ABC$ D & E are two points on AB & AC such that

$$AD = 4 \text{ cm}$$

$$AE = 5 \text{ cm}$$

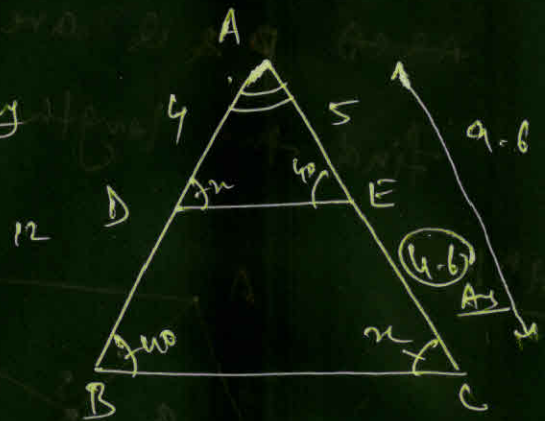
$$AB = 12 \text{ cm}$$

$$BC = 40$$

$$\angle CED = 140$$

$$\angle C = ?$$

Ans



$$\triangle ADE \sim \triangle ABC$$

$$LE = 40$$

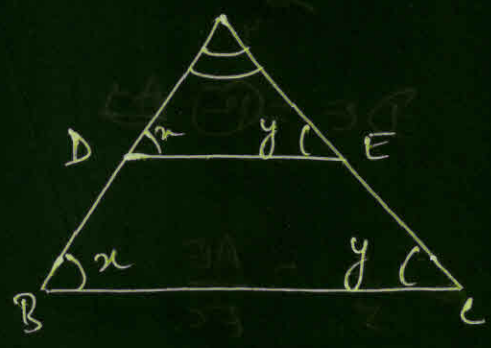
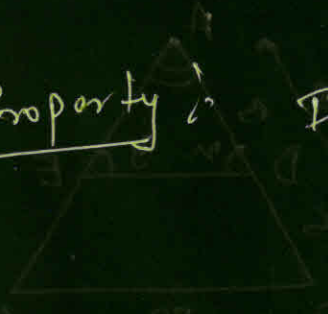
$$\angle A = \angle A$$

$$\frac{AC}{AD} = \frac{AB}{AE}$$

$$\frac{AC}{4} = \frac{12}{5}$$

$$A = \frac{48}{6} = \underline{9.6}$$

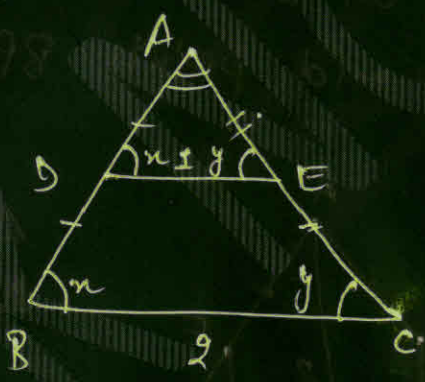
① Property: In a triangle ABC, DE || BC



$$\frac{AD}{AB} = \frac{AE}{AC} = \frac{DE}{BC}$$

$$\frac{AD}{BD} = \frac{AE}{EC}$$

② In a triangle ABC, D & E are the mid points of AB & AC then



$\Delta ADE \sim \Delta ABC$
 $DE \parallel BC$

$$DE = \frac{BC}{2}$$

Q1. In a triangle ABC, DE || BC, then

- ① AD = 3
- BD = 5
- BC = 32
- DE = ?

- ② AD = 3
- BD = 5
- EC = 32
- AE = ?



A-0

$$\frac{DE}{BC} = \frac{AD}{AB} = \frac{DE}{32} = \frac{3}{8}$$

$$DE = \frac{12}{8} \times 32 = 48 \text{ cm}$$



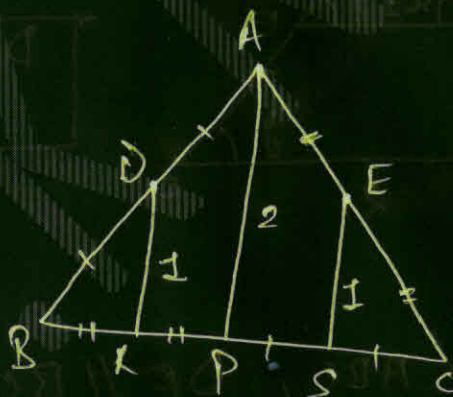
A-2

$$\frac{AD}{BD} = \frac{AE}{EC} = \frac{3}{5} = \frac{AE}{EC}$$

$$\frac{96}{5} = 19.2 \text{ cm}$$

Q1:- In a $\triangle ABC$ D & E are mid points of AB & AC. P is a point on BC such that BP:PC is 3:2, R & S are the mid points BP & PC find DR:ES.

Ans:-



$\triangle APB$

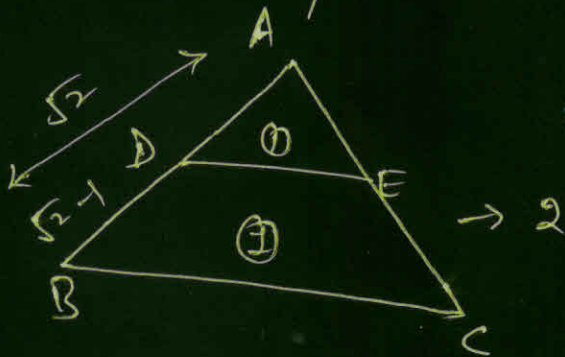
DR:ES

$\triangle APC$

1:1 Ans

Q2

In a $\triangle ABC$ DE || BC such that it divides $\triangle ABC$ into 2 equal area find AD:BD.



$$\sqrt{\frac{1}{2}} = \sqrt{\left(\frac{AD}{AB}\right)^2}$$

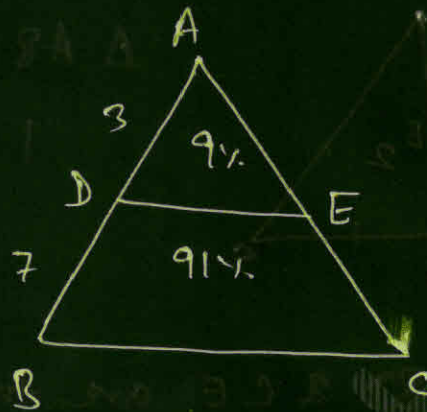
$$\frac{AD}{AB} = \frac{1}{\sqrt{2}}$$

$$AD:BD$$

$$1:\sqrt{2}-1 \text{ Ans}$$

Q:- In a $\triangle ABC$ $DE \parallel BC$ Such that $AD:BD$ is $3:7$.
 Find the Percentage % Area of Quadrilateral
 BDEF.

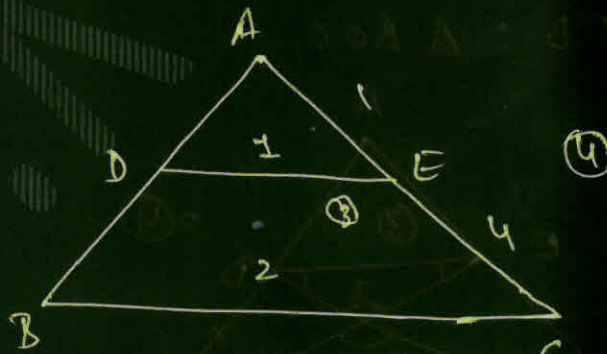
Ans:-



$$\frac{\text{area of } \triangle ADE}{\text{area of } \triangle ABC} = \left(\frac{AD}{AB}\right)^2$$

Q:- In a $\triangle ABC$, D & E are the mid points AB & AC. then find the % area of Quadrilateral BDEC.

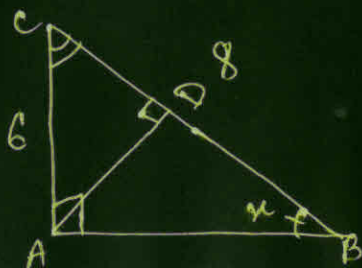
Ans:-



$$\frac{3}{4} = 75\% \text{ Ans}$$

Q:- In a $\triangle ABC$, $\angle A = 90^\circ$, $AD \perp BC$ of $BC = 8 \text{ cm}$,
 $AC = 6 \text{ cm}$ - then find the Ratio of Area of $\triangle ABC$
 or $\triangle ACD$.

soln:-



$$\triangle ADC \sim \triangle ABC$$

$$90 = 90$$

$$\triangle ABC = \triangle ADC$$

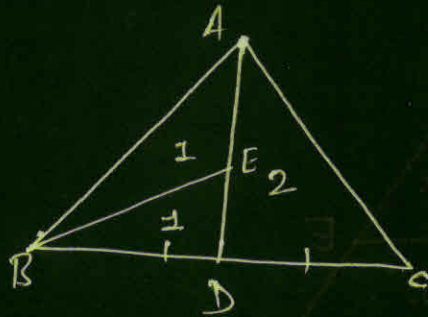
$$(8)^2 = (6)^2$$

$$64 = 36 + 9$$

$$\boxed{116:9} \text{ Ans}$$

Q: In $\triangle ABC$ D is the mid point of BC & E is mid point of AD then find the Ratio of Area of $\triangle AEB$ & $\triangle ABC$

Soln:



$$\triangle ABE : \triangle ABC$$

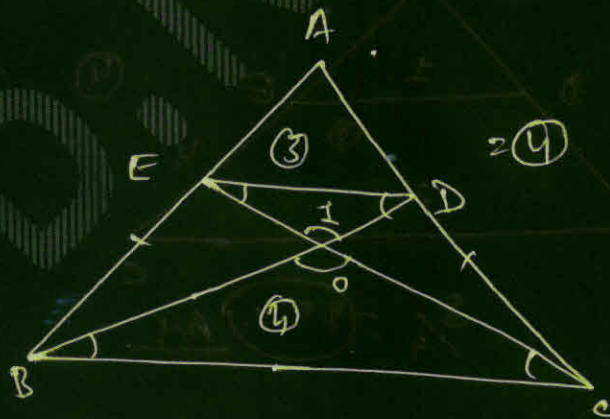
$$1 = 4 \text{ Ans}$$

Q: In $\triangle ABC$ BD & CE are two medians which intersect each other at point O. find the Ratio of the areas of $\triangle EOD : \triangle BOC$ & $\triangle AED$; $\triangle BOC$;

$$\textcircled{1} \triangle EOD : \triangle BOC$$

$$\textcircled{2} \triangle AED : \triangle BOC$$

Ans:



$$\triangle EOD : \triangle BOC$$

$$1 : 4$$

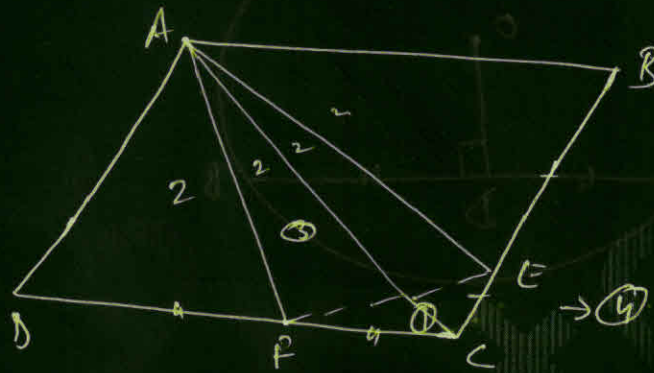
$$\triangle AED : \triangle BOC$$

$$3 : 4$$

$$\square \triangle AED = \triangle BOC = 4$$

Q: ABCD is parallelogram, E & f are the mid point of BC and CD. find the ratio of area of ΔAFE & ΔEFC .

Ans



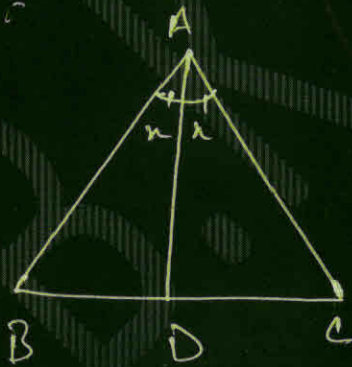
$\Delta AFE : \Delta EFC$

$3 : 1$

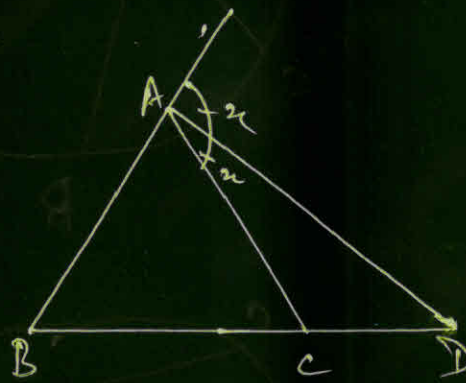
Ans

2	2
2	1

⇒ Property:



$$\frac{AB}{AC} = \frac{BD}{CD}$$

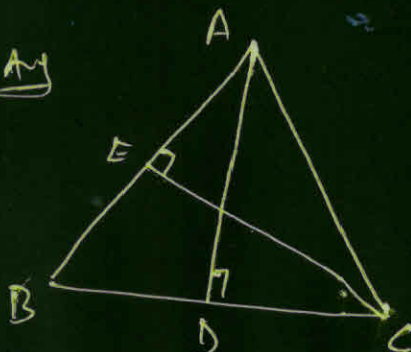


$$\frac{AB}{AC} = \frac{BD}{CD}$$

Q: In ΔABC , $AD \perp BC$ & $EC \perp AE$

then if
 $AB = 16$
 $CE = 24$
 $BC = 32$
 $AD = ?$

Ans

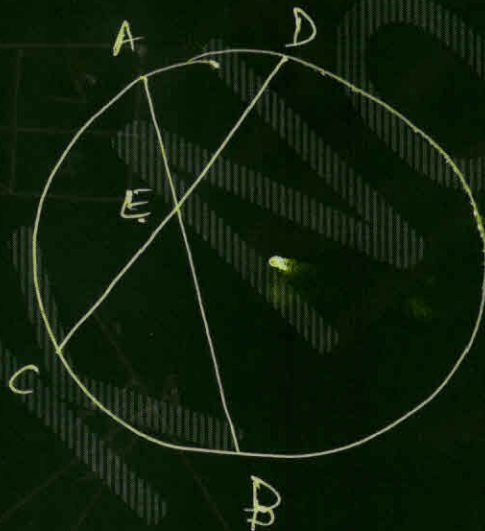
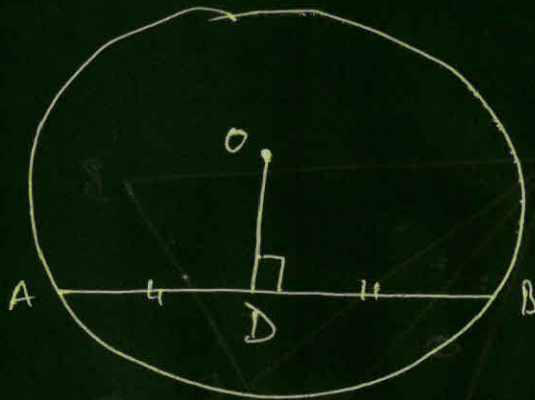


$$\frac{1}{2} \times BC \times AD = \frac{1}{2} \times AB \times CE$$

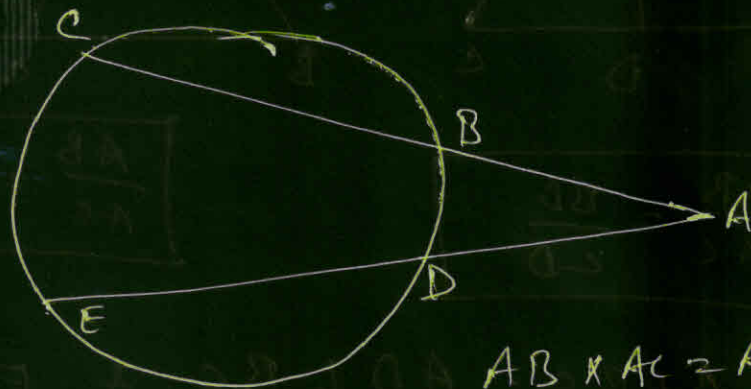
$$32 \times AD = 16 \times 24$$

$AD = 12$ Ans

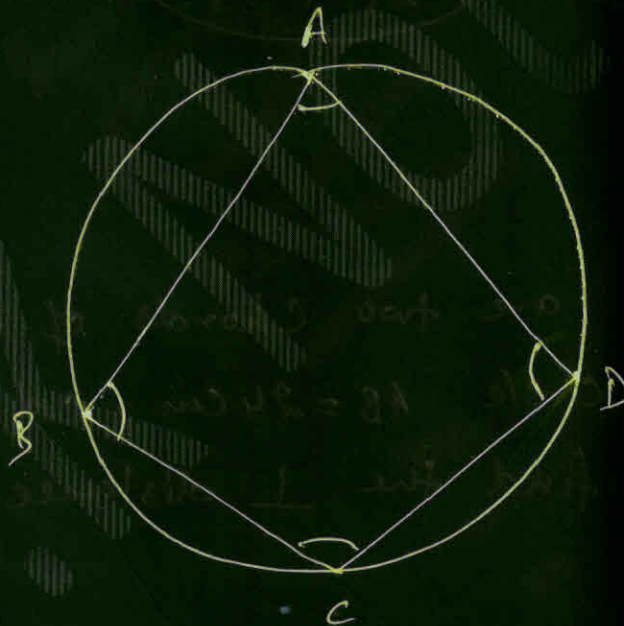
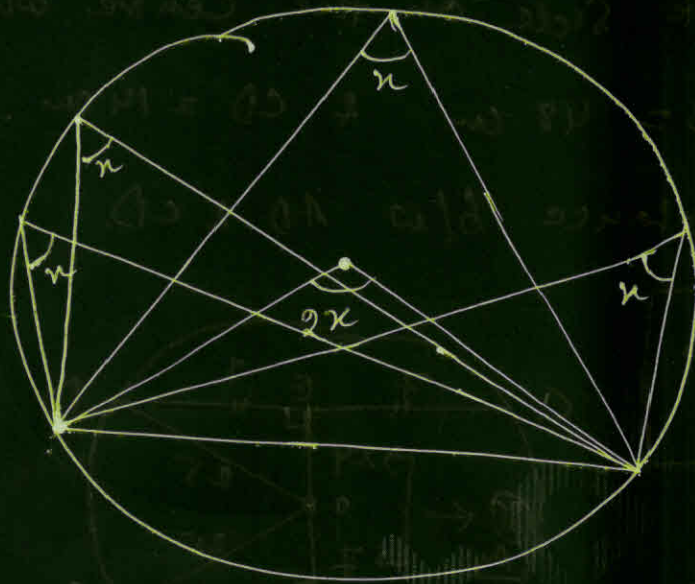
Circle



$$AE \times EB = CE \times ED$$

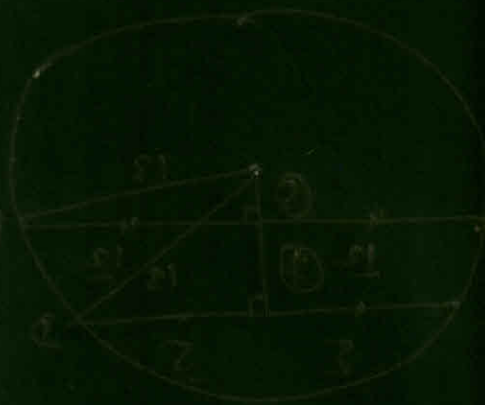


$$AB \times AC = AD \times AE$$



$$\angle A + \angle C = 180^\circ$$

$$\angle B + \angle D = 180^\circ$$

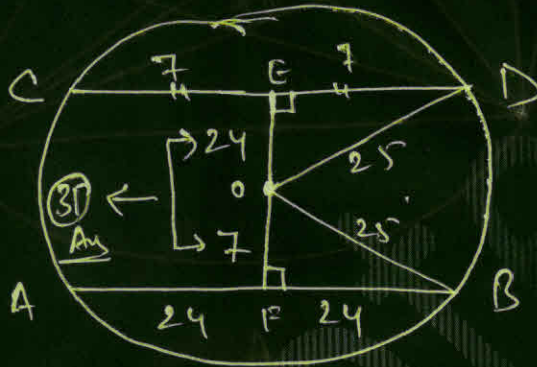


Q1- AB & CD are two chords of the circle of the opposite side on the centre which radius 25cm
 AB = 48 cm & CD = 14 cm. find the \perp

Soln 1- distance b/w AD & CD.

Learn Pythagoras Triplate

7, 24, 25



$$(ED)^2 + (OE)^2 = (OD)^2$$

$$(7)^2 + (OE)^2 = (25)^2$$

$$49 + (OE)^2 = 625$$

$$(OE)^2 = 576$$

$$24 = OE$$

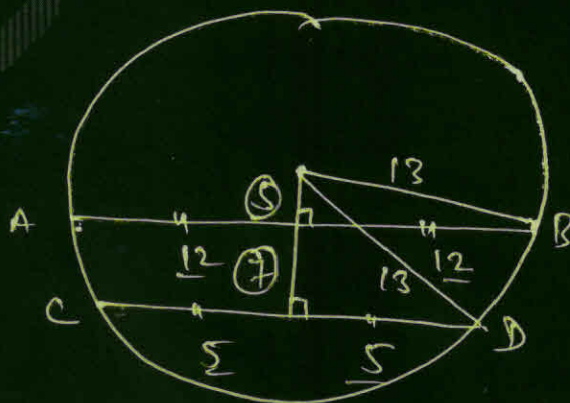
$$7 = OF$$

$$OE + OF$$

$$24 + 7 = 31 \text{ Ans}$$

Q2- AB & CD are two chords of the on the same side of circle AB = 24 cm, CD = 10 cm & radius = 13 cm. find the \perp distance AB & CD.

Soln 1-

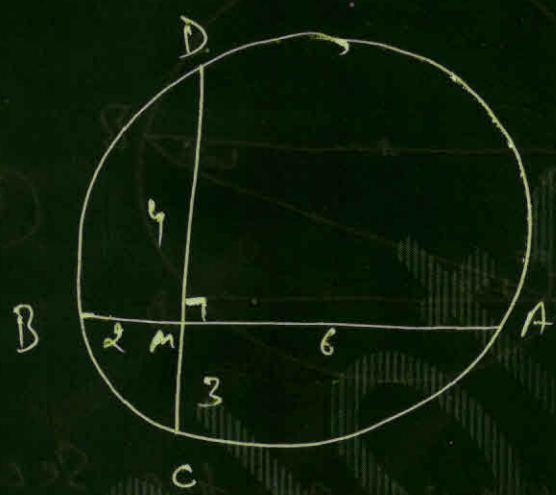


5

7 Ans

Q1) Find the Radius of circle in which AB and CD are 2 chords which intersect each other at right angles at point M. If AM = 6cm, CM = 3cm and MD = 4cm.

Soln.



$$AM \times MB = CM \times MD$$

$$6 \times MB = 3 \times 4$$

$$MD = 2$$

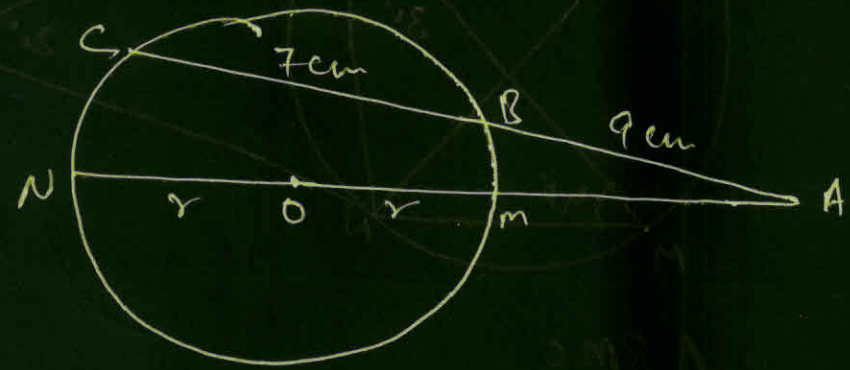
$$D = \sqrt{6^2 + 2^2 + 3^2 + 4^2}$$

$$D = \sqrt{65}$$

$$R = \frac{\sqrt{65}}{2} \text{ Ans}$$

Q2) ABC & AMN are two secant of circle with centre O. MN is the diameter. If AB = 9cm, BC = 7cm & AO = 13cm find the Radius.

Soln.



$$AO = 13$$

$$AM = 13 - r$$

$$AN = 13 + r$$

$$AB \times AC = MA \times AN$$

$$9 \times 16 = (13 - r)(13 + r)$$

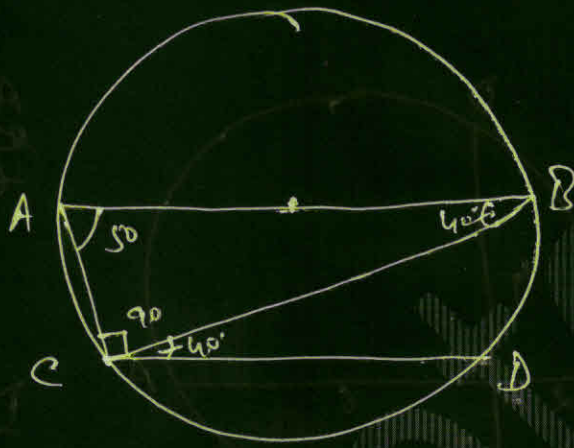
$$144 = 169 - r^2$$

$$+25 = r^2$$

$$r = 5 \text{ Ans}$$

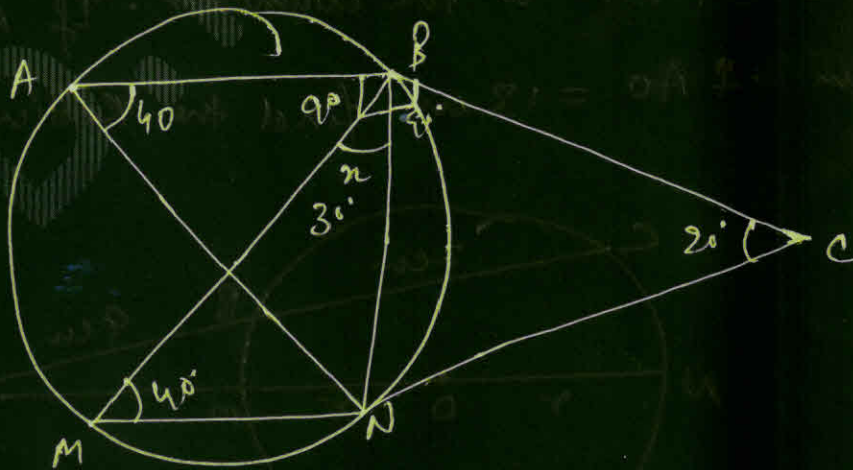
Q1 AB is the diameter of the circle & CD is a chord parallel of AB. If Angle $\angle BAC = 50^\circ$ then find $\angle BCD = ?$

Soln



40 Ans

Q1 ABC and MNC are two Secants of the circle with the centre O. AN is diameter $\angle C = 20^\circ$ AND $\angle BAN = 40^\circ$ find $\angle MBN = ?$



$\triangle BMC$

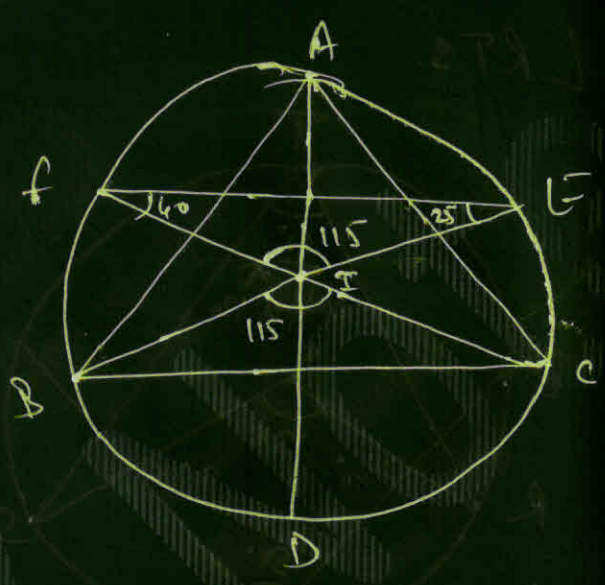
$$\angle M + \angle C + \angle B = 180^\circ$$

$$40 + 20 + 90 + n = 180^\circ$$

$n = 30^\circ$ Ans

Q1:- ABC is a triangle drawn inside a circle. the Angle bisector of LA, LB and LC intersect the Circumference at the point D, E & F. If LA = 50° & LCFE = 40°. find Angle LBFE = ?

Soln:-



or

$$\angle BIC = 90 + \frac{\angle A}{2}$$

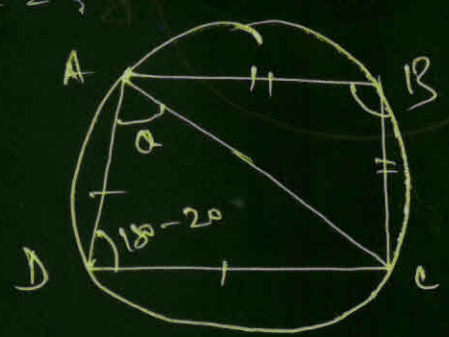
$$\angle BIC = 115^\circ$$

$$\Rightarrow \angle FIE = 115^\circ$$

$$\text{So, } \angle FEB = 180^\circ - 40^\circ = \underline{140^\circ} \text{ Ans}$$

Q2:- ABCD is a cyclic quadrilateral such that AB = BC & AD = CD. If Angle CAD = 20°. find LABC = ?

Soln:-



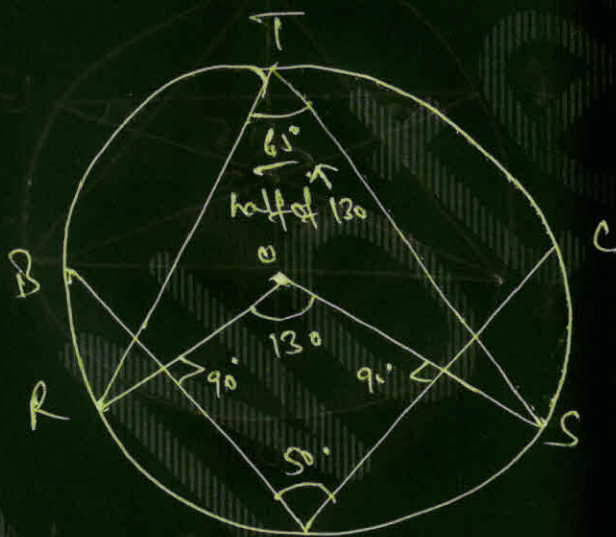
$$\angle B + \angle D = 180^\circ$$

$$\angle B + 180^\circ - 20^\circ = 180^\circ$$

$$\boxed{\angle B = 20^\circ} \text{ Ans}$$

Q1) AB & AC are two chords of circle with the centre O. P & Q are mid points of AB & AC. OP & OQ are extended upto points R & S of the circumference of the circle T is the point on major arc RS. If $\angle A = 50^\circ$. then find $\angle RTS$.

Solⁿ



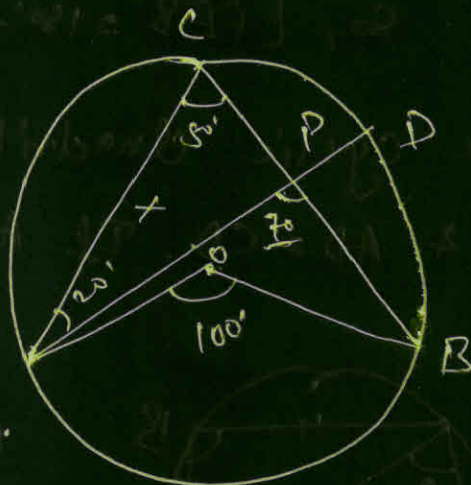
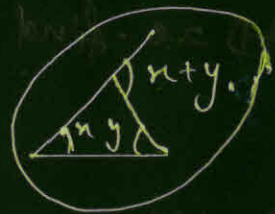
$$\angle A + \angle O = 180^\circ$$

$$\angle O = 180 - 50^\circ = 130^\circ$$

half of 130° is 65° that's Answer

Q2) AD and BC are two chords of a circle which intersect each other at point P and O is centre. If $\angle AOB = 100^\circ$, $\angle CAD = 20^\circ$ then find $\angle APB = ?$

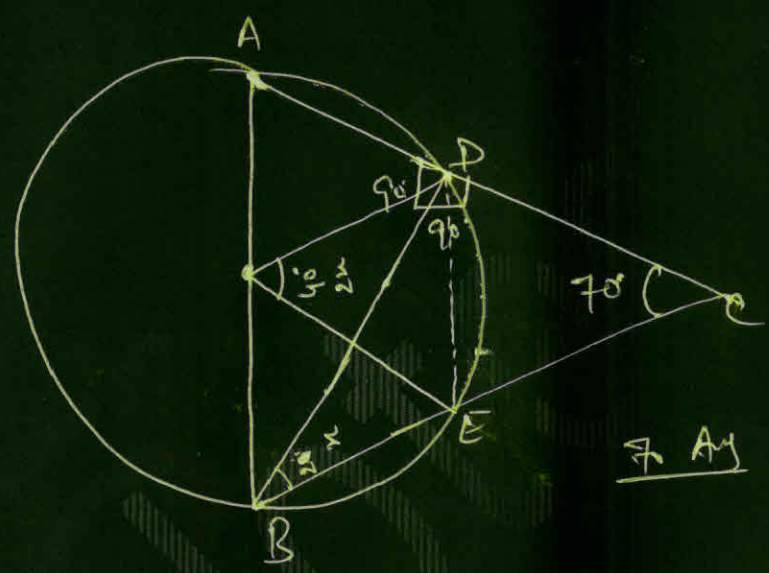
Solⁿ



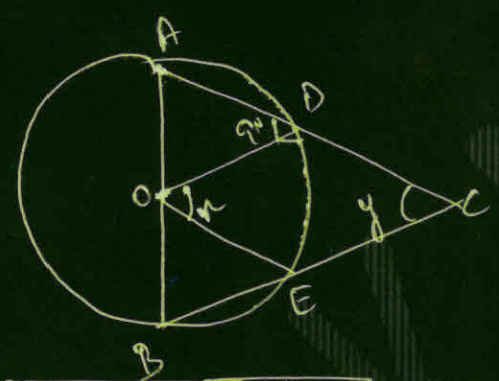
70° Ans

Q1: AB is the diameter & O is centre of circle ADC & BEC are two secants if $\angle DOE = 240^\circ$ then find $\angle C = ?$

Solⁿ:



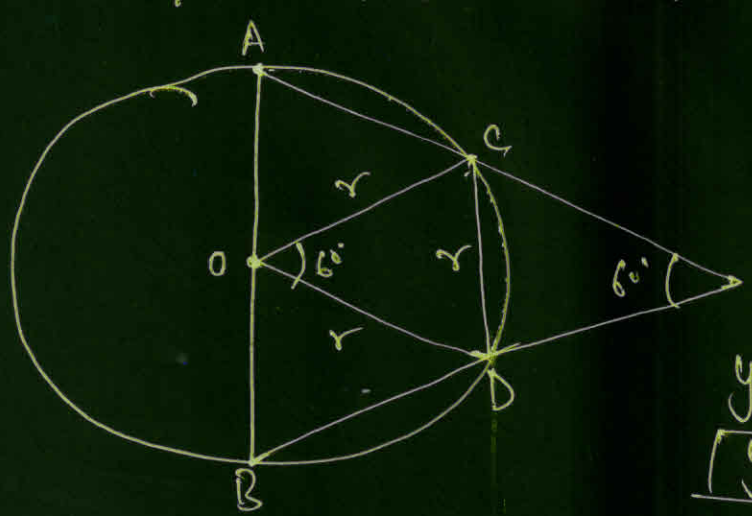
Property



$$y = 90 - \frac{x}{2}$$

Q1: AB is the diameter & O is the centre of the circle. CD is chord parallel as well as half of AB. the sides AC & BD are extended which intersect each other at point T outside the circle find $\angle T = ?$

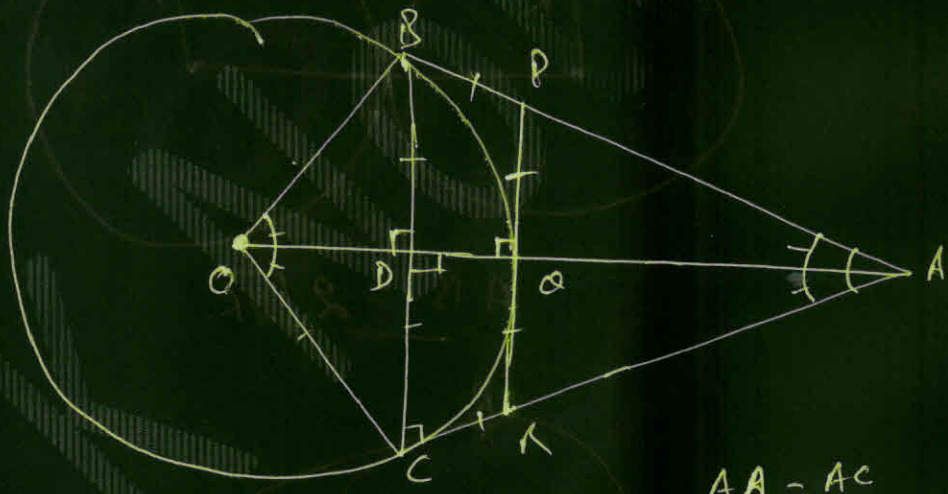
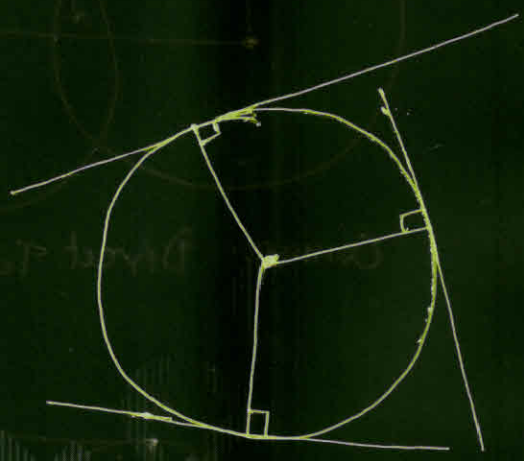
Solⁿ:



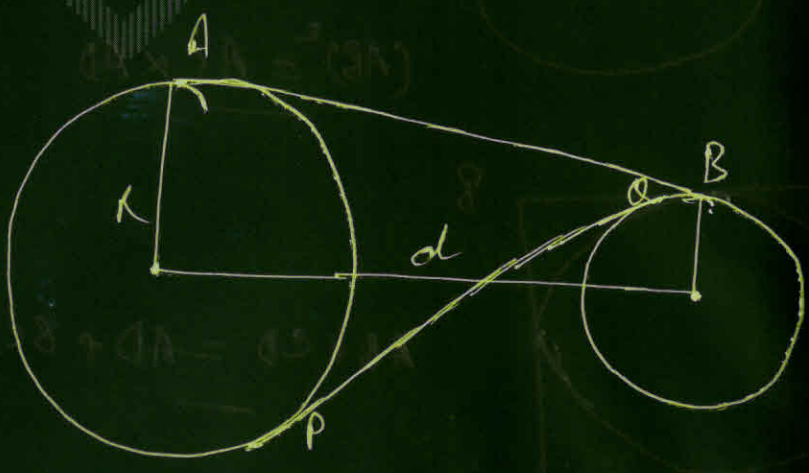
$$y = 90 - \frac{60}{2}$$

$$\boxed{y = 60^\circ} \text{ Ans}$$

* — TANGENT — *

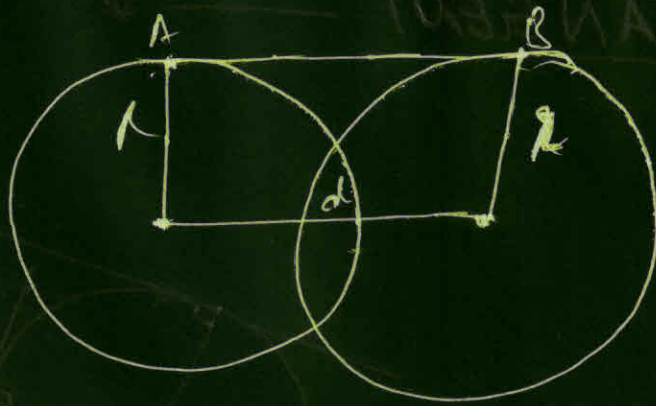


$AB = AC$
 $\angle A + \angle O = 180^\circ$
 $BD = CD$
 $BP = PO = OR = RC$

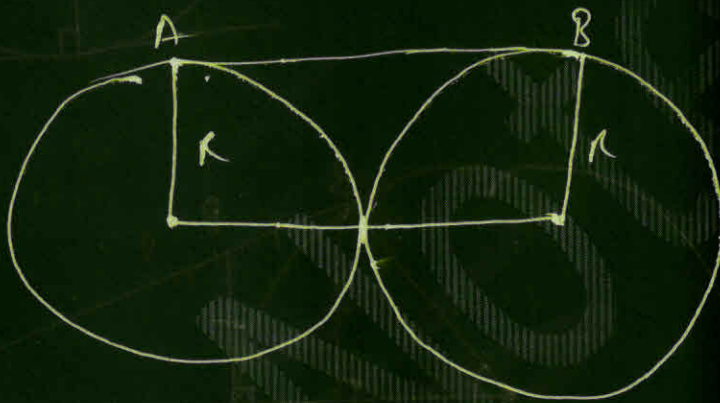


Common Direct Tangent (AB) = $\sqrt{d^2 - (R^2 - r^2)}$

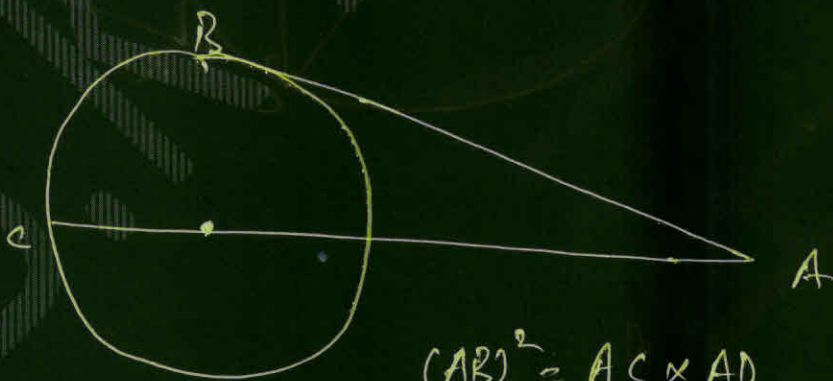
Common Transverse tangent (PQ) = $\sqrt{d^2 - (R + r)^2}$



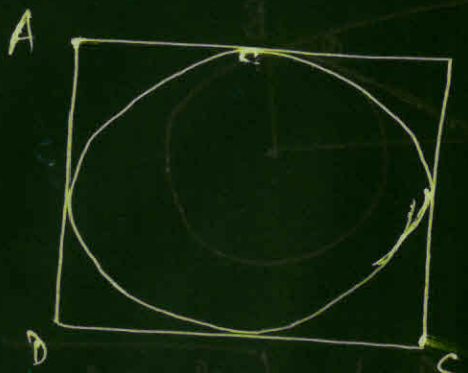
Common Direct Tangent (AB) = $\sqrt{d^2 - (r-r)^2}$



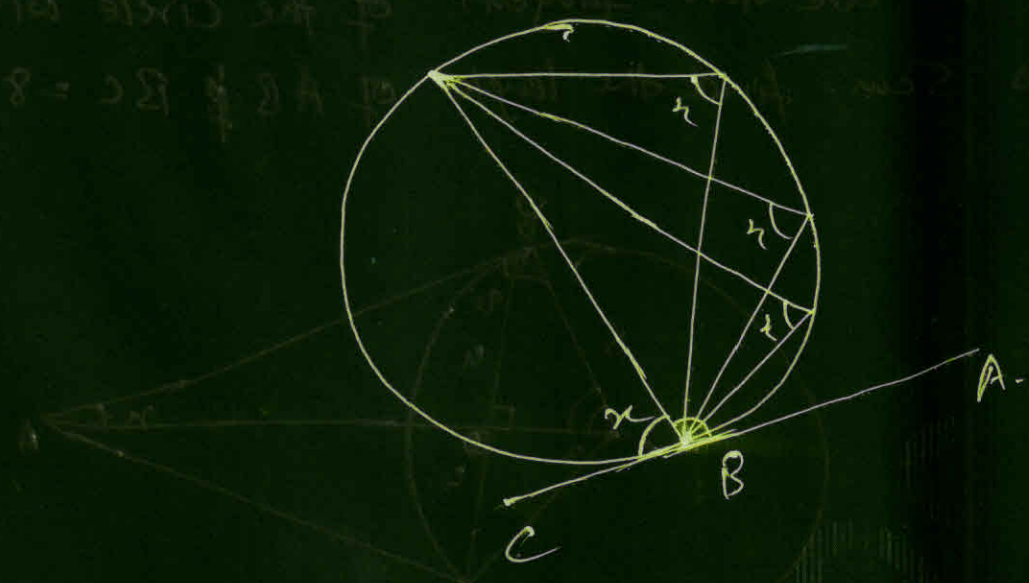
AB = $2\sqrt{2r}$



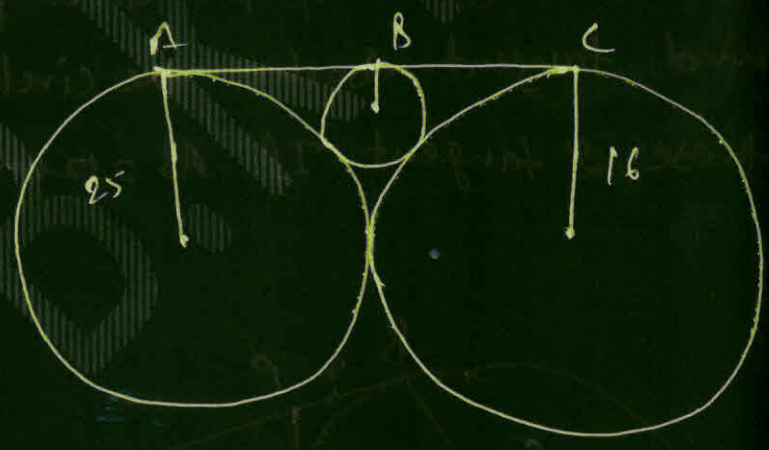
$(AB)^2 = AC \times AD$



AB + CD = AD + BC



Q6 Two circles with the radius 25 cm & 16 cm touch each other externally a third circle with radius x touches these two circles as well as their common tangent. find x .



$$AB = 2\sqrt{25 \times x} = 10\sqrt{x}$$

$$BC = 2\sqrt{16 \times x} = 8\sqrt{x}$$

$$AC = 2\sqrt{25 \times 16} = 40$$

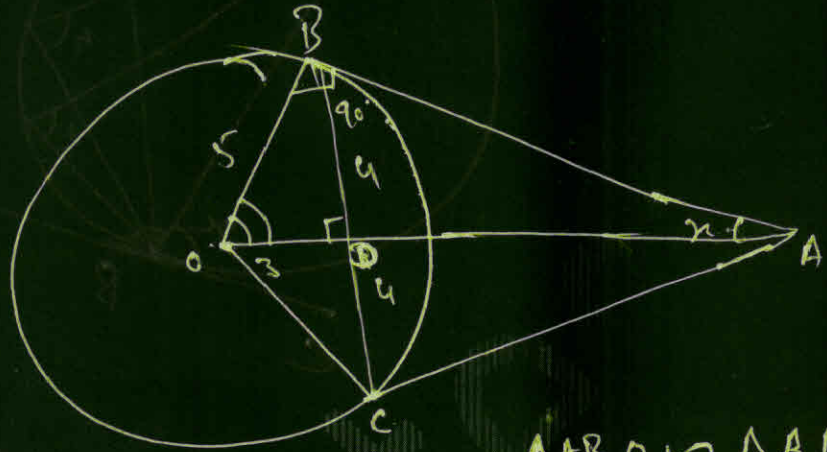
$$AB + BC = AC$$

$$10\sqrt{x} + 8\sqrt{x} = 40$$

$$\sqrt{x} = \frac{20}{9}$$

$$\Rightarrow \boxed{x = \frac{400}{81}} \text{ Ans}$$

Q1: AB & AC are two tangent of the circle with the radius 5cm. find the length of AB if BC = 8cm.
Solⁿ

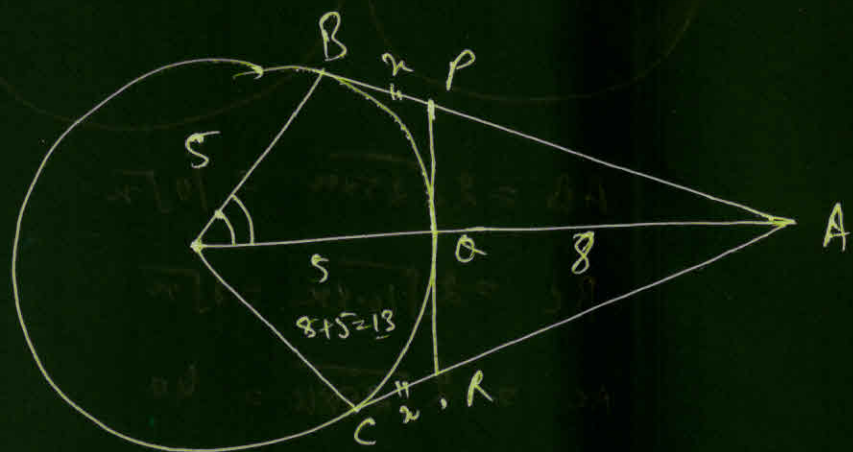


$$\triangle ABO \sim \triangle BDO$$

$$\frac{AB}{BD} = \frac{BO}{OD}$$

$$\frac{AB}{5} = \frac{4}{3} = \left(\frac{20}{3}\right) \text{ Ans}$$

Q2: AB & AC are two tangent of the circle find the length of third tangent touches the circle as well as intersect those 2 tangent If AB = 12cm & radius is 5cm.
Solⁿ



$$\triangle ABO \sim \triangle BDO$$

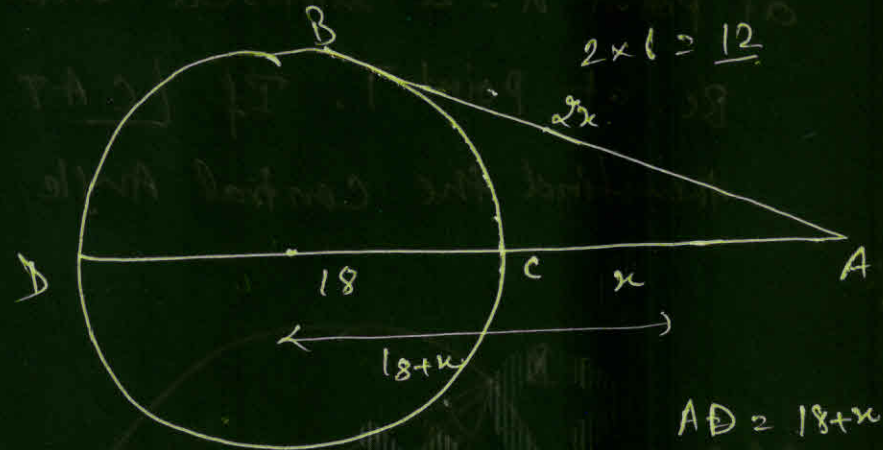
$$(12-x)^2 = x^2 + 18^2$$

$$x = \frac{10}{3}$$

$$PR = \frac{10}{3} + \frac{10}{3} = \left(\frac{20}{3}\right) \text{ Ans}$$

Q: AB is a tangents. ACD is secant of the circle such that $AB = 2AC$. and $CD = 18$ cm find AB.

$AB = 2x$
 $AC = x$



$(AB)^2 = AC \times AD$

$(2x)^2 = x + (x + 18)$

$4x^2 = x^2 + 18x$

$3x^2 = 18x$

$x = 6$

$2 \times 6 = 12$ Ans

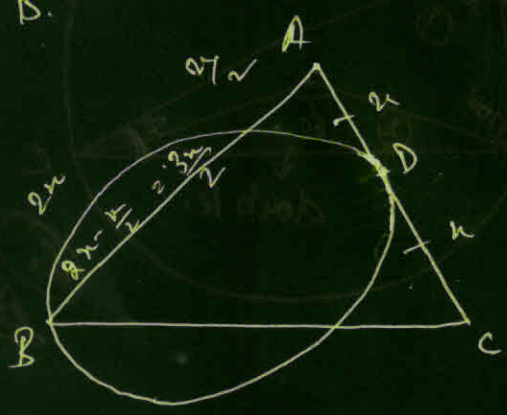
Q: ΔABC is a triangle in which $AB = AC$. A circle passes to point B & touches side AC at its mid point. D & intersect side AB at point P. find AP Ratio PB.

Soln:

$(AD)^2 = AP \times AB$

$(x)^2 = AB \times \frac{3x}{2}$

$AP = \frac{x}{2}$



$AB = AC = 2x$

$AP = PB$

$\frac{x}{2} = \frac{3x}{2}$

1 : 3 Ans

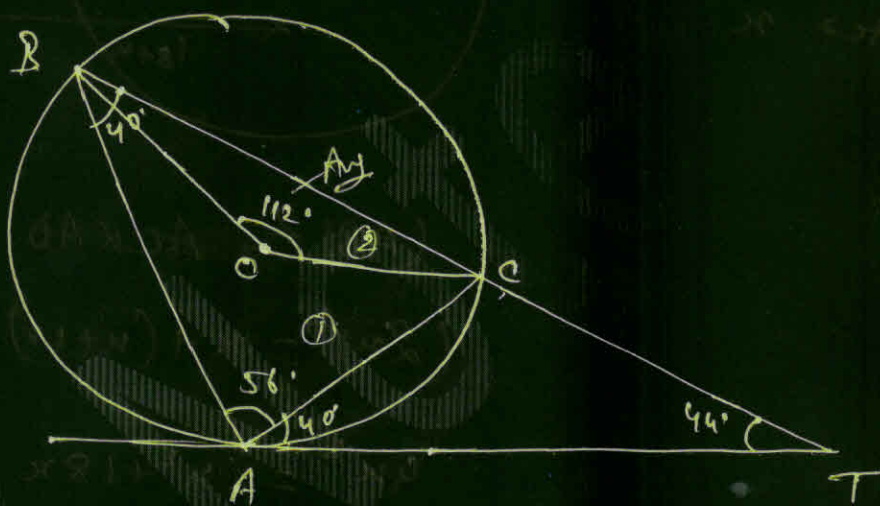
Q1:- ABC are Three points of Circumference of the circle such that a tangent touches the circle at point A & Intersect extended part of Chord BC at point T. If $\angle CAT$ is 40° & $\angle CTA = 44^\circ$ then find the central Angle made by chord BC.

Ans 6

$$\triangle BAC = 2 \triangle BOC$$

$$56 = 56 \times 2$$

$$56 = \underline{112^\circ} \text{ Ans}$$



Q2 AD is a tangent & ABC is secant of circle where AB = BD side BA is extended upto point E. $\angle OAE$ is 130° ; then find the central Angle made by chord BC.

